

# Capturing Macroeconomic Tail Risks with Bayesian Vector Autoregressions

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## How do we measure (negative) tail risks to macroeconomic outcomes?

- Rapidly growing lit focused on GDP growth and quantile regression: Adrian, Boyarchenko, and Giannone (2019, ABG), Adrian, et al. (2018), Giglio, Kelly, and Pruitt (2016)
  - Focus on risks associated with poor financial conditions

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  - Focus on risks associated with poor financial conditions
- Some work considers risks to unemployment (e.g., Galbraith and van Norden 2019, Kiley 2018) or inflation
- Some work considers other methods, such as copula
- Other work drills deeper to better understand tail risks: Loria, Matthes, and Zhang (2019) examine drivers of left tail

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- Monetary policymakers have commonly treated forecast distributions as being potentially asymmetric, at some points in time

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- ABG and others sometime refer explicitly to conditional: recessions associated with left-skewed distributions
- But one pattern that has been emphasized — downside risk varying more than upside — could occur with predictive distributions that are symmetric

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- But one pattern that has been emphasized — downside risk varying more than upside — could occur with predictive distributions that are symmetric
- Need simultaneous mean and variance shifts
- Simple example: shift from  $N(0,1)$  to  $N(-2,4) \Rightarrow$  95% quantile edges down from 1.65 to 1.29, whereas 5% quantile drops from -1.65 to -5.29.



We examine the ability of BVARs with stochastic volatility (SV) to capture tail risks in macroeconomic forecast distributions and outcomes

- BVARs have a known track record and can be used for a range of forecasting purposes
- BVAR-SV models commonly improve on the point and density forecast accuracy of their homoskedastic counterparts

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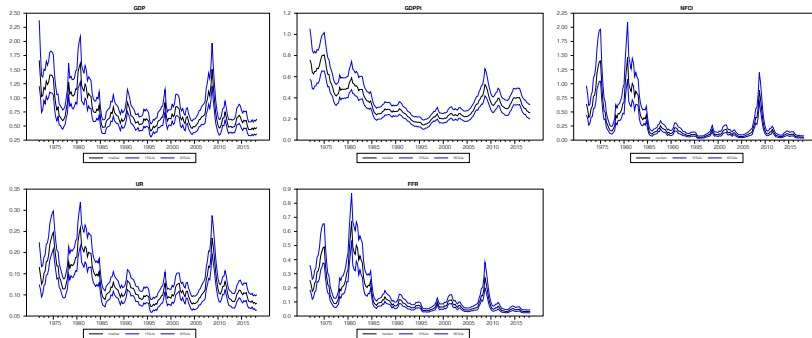
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BVAR-SV models have the potential to capture time-varying tail risks

- Due to simultaneous shifts in conditional means and variances
- Even though conditional distributions are symmetric (1-step, not necessarily multi-step)

# Introduction

Innovation volatility estimate: BVAR-SV model, N=5  
(standard deviation)



## Our models:

- Include 4 primary macroeconomic indicators and the NFCI indicator of financial conditions
- Focus on risks to GDP growth
- Include conventional BVAR-SV and a BVAR with a generalized factor structure to volatility in which the common factor is a function of past financial conditions
- Robustness checks:
  - Models with 2 and 15 variables
  - Models replacing NFCI with an indicator of financial volatility
  - Forecasting unemployment instead of GDP growth

We provide more formal evaluations of asymmetries and risk forecasts than has much of the recent literature

- Formal tests of skewness in the data, BVAR residuals, and forecast errors
- Formal scoring of quantile and expected shortfall forecasts
  - Conventional quantile scoring function
  - More recent joint scoring function for the quantile and its associated expected shortfall
- BVAR-SV vs. ABG-style quantile regression

## Related contemporaneous paper: Caldara, Scotti, and Zhong (2019)

- Our focus is more on forecasting with VARs like those common in the literature, including formal scoring comparisons
- They focus more on using a bivariate VAR with an explicit correlation in shocks to levels and volatilities to produce time-varying asymmetries in conditional predictive distributions

## Main findings

- Formal statistical evidence of skewness in output growth is generally weak

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- Formal statistical evidence of skewness in output growth is generally weak
- QR-based approaches can come with some challenges in macro data samples: quantile crossing and coefficient variability
- BVAR-SV models are able to capture time variation in output tail risks — with downside risks more variable than upside risks — like that emphasized in ABG
  - SV crucial
- BVAR-SV and BVAR-GFSV models score about as well as QR for downside tail risks

## 1 Models

# Outline

1 Models

2 Data

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- 3 Forecast Metrics

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- 5 Conclusions

$$y_t = \sum_{i=1}^p \Pi_i y_{t-i} + v_t$$

$$v_t = A^{-1} \Lambda_t^{0.5} \epsilon_t, \quad \epsilon_t \sim N(0, I_n), \quad \Lambda_t \equiv \text{diag}(\lambda_{1,t}, \dots, \lambda_{n,t})$$

$$\ln(\lambda_{i,t}) = \gamma_{0,i} + \gamma_{1,i} \ln(\lambda_{i,t-1}) + \nu_{i,t}, \quad i = 1, \dots, n$$

$$\nu_t \equiv (\nu_{1,t}, \nu_{2,t}, \dots, \nu_{n,t})' \sim N(0, \Phi)$$

- $\Lambda_t$  contains the time-varying variances of conditionally Gaussian shocks
- $A$  is uni-triangular
- Reduced-form VCV is  $\text{var}(v_t) \equiv \Sigma_t = A^{-1} \Lambda_t A^{-1'}$

# Models: BVAR-GFSV model

Incorporates a factor structure of volatility in a VAR-SV (CCM 2016, 2017) and links the volatility factor to the lagged NFCI

- Allows a link of poor financial conditions to elevated macroeconomic uncertainty and volatility, capturing the basic idea of ABG
- Each variable's log vol. follows a linear factor model with a common uncertainty factor  $\ln m_t$  and an idiosyncratic component  $\ln h_{i,t}$
- Generalizes a much simpler model of a robustness check in ABG

$$y_t = \sum_{i=1}^p \Pi_i y_{t-i} + A^{-1} \Lambda_t^{0.5} \epsilon_t$$

$$\ln \lambda_{i,t} = \beta_{m,i} \ln m_t + \ln h_{i,t}, \quad i = 1, \dots, n$$

$$\ln m_t = \sum_{i=1}^{p_m} \delta_{m,i} \ln m_{t-i} + \delta_f \text{NFCI}_{t-1} + u_{m,t}, \quad u_{m,t} \sim iid N(0, \phi_m)$$

$$\ln h_{i,t} = \gamma_{i,0} + \gamma_{i,1} \ln h_{i,t-1} + e_{i,t}, \quad i = 1, \dots, n$$



# Models: Priors and Estimation

## SV Priors:

- VAR coefficients  $\Pi$ : Normal, with Minnesota-style prior, means of 0
- $A$ , row by row: Normal, prior mean of 0 and variance  $10 \cdot I$
- SV process: Normal, with  $\gamma_{i,1}$  having mean of 0.9 and st. dev. of 0.2
- $\Phi$ : IW with mean of  $0.03 \cdot I$  and 10 df

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## Symmetry?

- 1-step ahead predictive distributions are symmetric
- Multi-step predictive distributions don't have to be symmetric but are, empirically speaking

# Models: Quantile Regression

## Step 1 of 2: Conventional QR estimation

$$y_{t+h}^{(h)} = x_t' \beta + \epsilon_{t+h}$$

$$\hat{\beta} = \underset{\beta}{\operatorname{argmin}} \sum_{t=1}^{T-h} \left( \tau \cdot \mathbf{1}_{(y_{t+h}^{(h)} \geq x_t' \beta)} |y_{t+h}^{(h)} - x_t' \beta| + (1 - \tau) \cdot \mathbf{1}_{(y_{t+h}^{(h)} < x_t' \beta)} |y_{t+h}^{(h)} - x_t' \beta| \right)$$

- $h$  = forecast horizon of either 1 or 4 quarters
- $y_t = 400 \Delta \ln \text{GDP}_t$ ,  $y_{t+h}^{(h)} \equiv h^{-1} \sum_{i=1}^h y_{t+i}$
- $x_t$  includes a constant,  $y_t$ , and  $\text{NFCI}_t$
- Model estimated for quantiles of  $\tau = 0.05, 0.25, 0.75, 0.95$ , and  $0.5$ .

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## Step 2: Smooth the estimated quantile function by fitting a skewed- $t$ distribution

- Fit to quantiles of  $\tau = 0.05, 0.25, 0.75, 0.9$
- Use fitted distribution for computing expected shortfall, etc.

VARs include 5 variables: GDP growth, unemployment rate, inflation (GDP deflator), federal funds rate, NFCI

- Results similar with 2 and 15 variables
- Alternative financial measure and longer sample: turbulence measure of volatility from Giglio, Kelly, and Pruitt (2016)

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- In real-time evaluation, actuals = 1st release available in RTDSM

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Samples:

- Estimation with NFCI uses data starting in 1971, ending in 2018
- Estimation with turbulence uses data starting in 1959, ending in 2011
- Real time forecasts start in 1985 with NFCI and 1972 with turbulence



We consider both in-sample and OOS forecasts for small samples of bad outcomes and comparability to ABG

# Forecast Metrics

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Basic checks: RMSEs of point forecasts and log scores of forecasts

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Tail risks to GDP growth evaluated at  $\tau = 5\%$

- Results similar at  $\tau = 10\%$

## 5% quantile score

$$QS_{t+h} = (y_{t+h} - Q_{\tau,t+h})(\tau - \mathbf{1}_{(y_{t+h} \leq Q_{\tau,t+h})}),$$

where  $Q_{\tau,t+h}$  = forecast quantile at quantile  $\tau = 0.05$

- 5% quantile  $\equiv$  value at risk (VaR)

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## Expected shortfall (ES) and long-rise (LR)

- Shortfall = E(GDP growth in 5% tail)
- Long-rise = E(GDP growth in 95% tail)
- BVAR-SV: easily computed with draws from predictive distribution
- QR: Computed with complete skew- $t$  density functions from smoothing step

## Joint VaR-ES score:

- VaR-ES can be jointly elicited, but ES by itself cannot (Fissler and Ziegel 2016)
- We use the joint score of Fissler, Ziegel, and Gneiting (2015)

$$\begin{aligned} S_{t+h} &= Q_{\tau,t+h} \cdot (\mathbf{1}_{(y_{t+h} \leq Q_{\tau,t+h})} - \tau) - y_{t+h} \cdot \mathbf{1}_{(y_{t+h} \leq Q_{\tau,t+h})} \\ &+ \frac{e^{\text{ES}_{\tau,t+h}}}{1 + e^{\text{ES}_{\tau,t+h}}} (\text{ES}_{\tau,t+h} - Q_{\tau,t+h} + \tau^{-1} (Q_{\tau,t+h} - y_{t+h}) \mathbf{1}_{(y_{t+h} \leq Q_{\tau,t+h})}) \\ &+ \ln \frac{2}{1 + e^{\text{ES}_{\tau,t+h}}} \end{aligned}$$

# Results: Roadmap

Note: BVAR-GFSV estimates generally very similar to BVAR-SV

Tests of skewness

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Estimate of ES and LR: In-sample and out-of-sample forecasts

Formal assessment of forecast accuracy

Robustness checks

- Alternative measure of financial conditions: turbulence
- Alternative measure of economic activity:  $\Delta$  unemployment rate

## Results: Skewness

	skewness	Bai-Ng
<b>Data, 1972-2018</b>		
GDP growth	-0.364	-0.865
Unemployment	0.683	0.644
GDP inflation	1.402	1.995**
Fed funds rate	0.709	0.787
NFCI	1.979	2.016**

- Right column provides Bai and Ng (2005) time-series robust test statistic for skewness
- Raw data: skewness statistics are often large, but not necessarily statistically significant

## Results: Skewness

	skewness	Bai-Ng
<b>BVAR-SV resid., 1972-2018</b>		
GDP growth	0.237	0.406
Unemployment	0.542	1.073
GDP inflation	0.196	0.589
Fed funds rate	1.422	0.644
NFCI	-0.186	-0.258
<b>BVAR-SV resid./SV, 1972-2018</b>		
GDP growth	0.129	0.664
Unemployment	0.326	2.783***
GDP inflation	0.119	0.956
Fed funds rate	-0.119	-0.754
NFCI	0.341	2.557**

- BVAR-SV residuals: No evidence of skewness
- Normalized BVAR-SV residuals: Evidence of skewness increases some

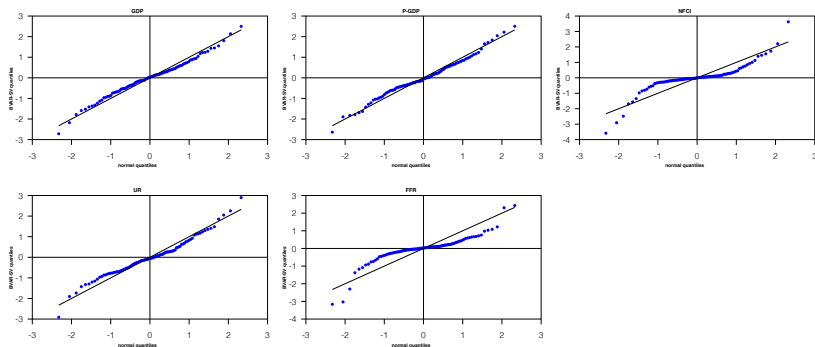
## Results: Skewness

	skewness	Bai-Ng
<b>BVAR-SV forecast errors, <math>h = 1Q</math>, 1985-2018</b>		
GDP growth	0.042	0.162
Unemployment	0.850	1.560
GDP inflation	-0.367	-1.839*
Fed funds rate	-0.115	-0.260
NFCI	1.632	0.826

- OOS forecast errors: A little evidence of skewness

# Results: Skewness

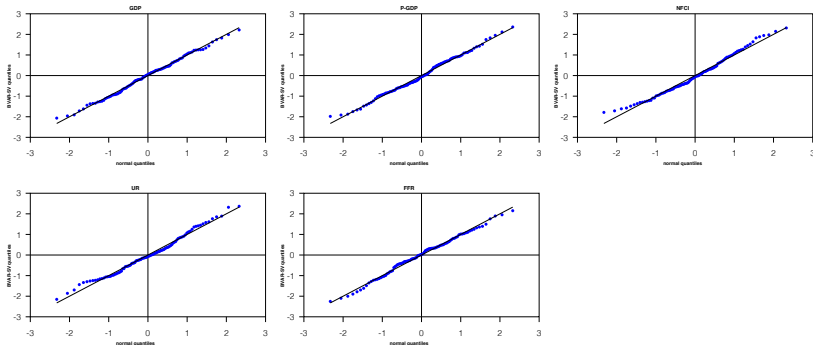
QQ plots of residuals from BVAR-SV model, N=5



- BVAR-SV residuals: Notable departures from normality, esp. for NFCI and FFR

# Results: Skewness

QQ plots of normalized residuals from BVAR-SV model, N=5

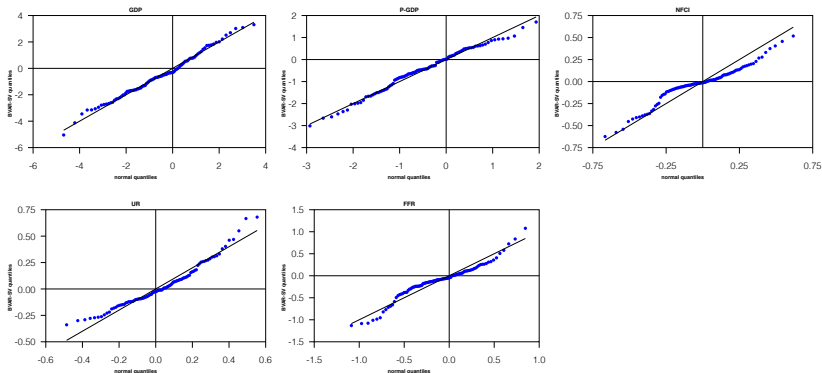


- Normalized BVAR-SV residuals: With normalization, departures from normality not so obvious



# Results: Skewness

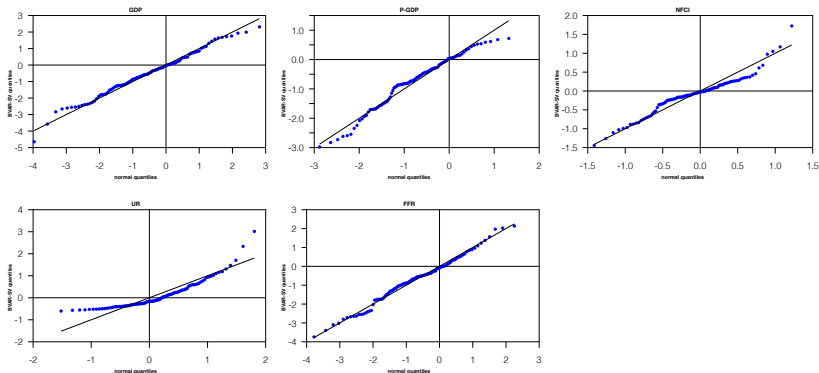
QQ plots of OOS forecast errors from BVAR-SV model, N=5  
forecast horizon = 1



- OOS BVAR-SV forecast errors, 1-step: As in not-normalized residuals, there are notable departures from normality

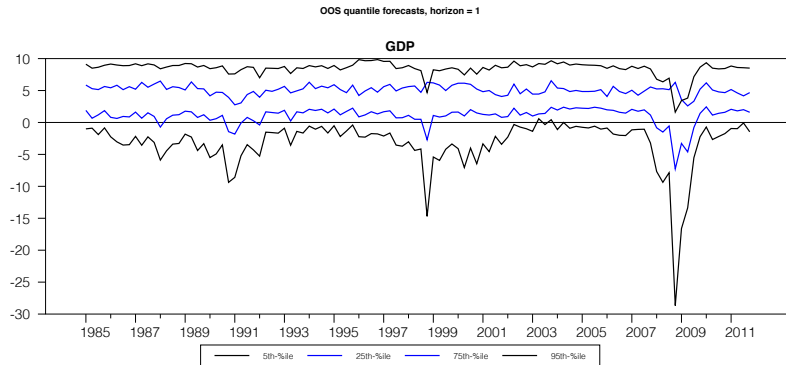
# Results: Skewness

QQ plots of OOS forecast errors from BVAR-SV model, N=5  
forecast horizon = 4



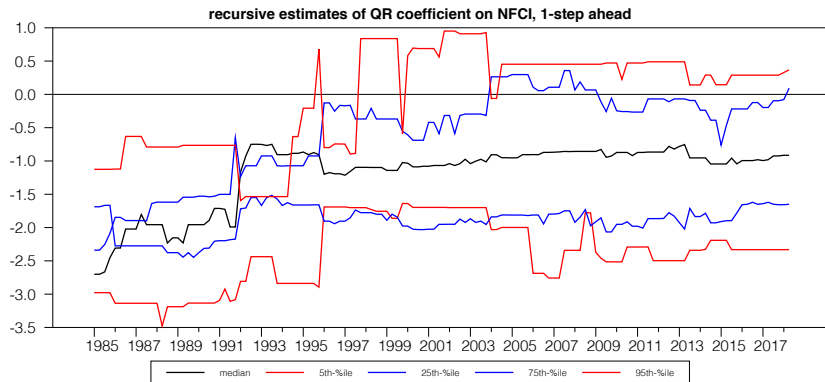
- OOS BVAR-SV forecast errors, 4-step: Again, there are notable departures from normality

# Results: Empirical challenges with QR



- In OOS estimates for GDP growth using turbulence (1-step), the 75th and 95th quantiles cross in two periods

# Results: Empirical challenges with QR



- In OOS estimates for GDP growth (1-step), the coefficient on  $NFCI_{t-1}$  can change sharply with the sample, esp. for the tail quantiles

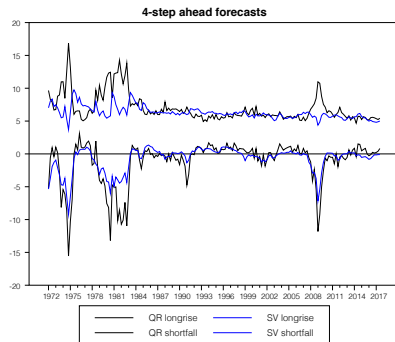
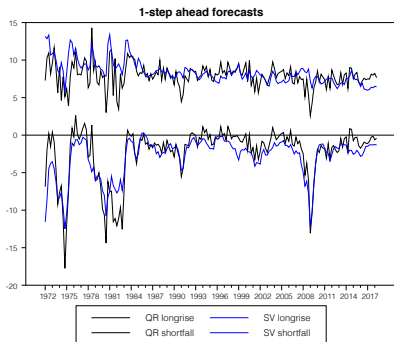
Small samples: Common to use extremal quantile methods for bias correction and inference

- Rule of thumb from Chernozhukov, Fernandez-Val, and Kaji (2017): extremal quantile methods should be used when  $\tau T/k \leq 15$  to 20, where  $\tau$  = quantile,  $T$  = sample size, and  $k$  = # regressors.
- GDP-NFCI application: with  $T = 160$ ,  $\tau = 0.05$ , and  $k = 3$ ,  $\tau T/k \approx 2.7$

# Results: Predictive distributions

## Expected longrise and shortfall: GDP growth

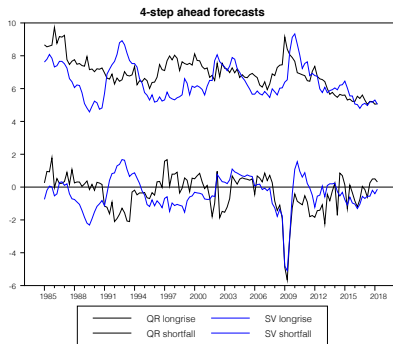
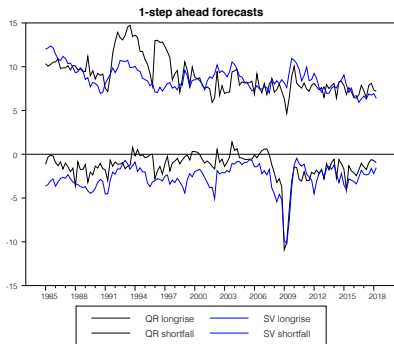
QR vs. BVAR-SV



- In-sample forecast estimates display asymmetries highlighted by ABG: ES variability  $>$  LR variability
- Pattern stronger at  $h = 1$  than  $h = 4$
- BVAR-SV comparable to QR, esp. at  $h=1$

# Results: Predictive distributions

## Expected longrise and shortfall: GDP growth QR vs. BVAR-SV



- Asymmetries still present but a little weaker OOS than in-sample
- QR-based estimates have some **upside** asymmetries in the 1990s
- OOS compared to IS: BVAR-SV estimates noisier; QR estimates less variable

## What drives the pattern in the BVAR estimates?

- Need SV to get conditional variance to move over time
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## What drives the pattern in the BVAR estimates?

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- Need financial conditions

## Monte Carlo experiments replicate variability of ES compared to LR

- Bivariate BVAR-GFSV based on GDP growth and NFCI
- BVAR-SV performance comparable to BVAR-GFSV

# Results: Accuracy of in-sample forecasts of GDP growth

	<b>BVAR-SV/QR</b>			
	1985-2018		1985-2007	
	$h = 1Q$	$h = 4Q$	$h = 1Q$	$h = 4Q$
RMSE	0.943	0.962	0.994	1.023
Log score	0.044*	0.031	0.004	-0.030
5% QS	0.982	1.081	1.031	1.100
5% VaR-ES	-0.073	-0.143	-0.151*	-0.227
	<b>BVAR-GFSV/QR</b>			
RMSE	0.942	0.958	0.988	1.013
Log score	0.051**	0.053	0.019	-0.010
5% QS	0.965	1.081	0.980	1.067
5% VaR-ES	-0.016	-0.073	-0.032	-0.112

- Conventional point and density forecasts: BVARs and QR broadly similar in accuracy
- Quantile score: Same
- VaR-ES score: Same, although GFSV sometimes better than SV and closer to QR performance

# Results: Accuracy of out-of-sample forecasts of GDP growth

	<b>BVAR-SV/QR</b>			
	1985-2018		1985-2007	
	$h = 1Q$	$h = 4Q$	$h = 1Q$	$h = 4Q$
RMSE	0.875*	0.873	0.867	0.819
Log score	0.062*	0.146	0.065	0.162
5% QS	1.099	0.877	1.158	0.767
5% VaR-ES	-0.251*	0.420	-0.355*	0.591
	<b>BVAR-GFSV/QR</b>			
RMSE	0.874**	0.872	0.860*	0.821
Log score	0.111***	0.176	0.122***	0.186
5% QS	0.982	0.801	0.989	0.689
5% VaR-ES	-0.104	0.651	-0.135	0.782

- OOS: In conventional point and density forecasts, BVARs beat QR
- Quantile score: BVAR-GFSV as good as or better than QR, BVAR-SV a little more mixed
- VaR-ES score: BVAR-GFSV comparable to QR, BVAR-SV not quite as good as GFSV

## Results: GDP growth forecast takeaways

QR doesn't seem to offer any advantages over BVAR-SV or BVAR-GFSV specifications

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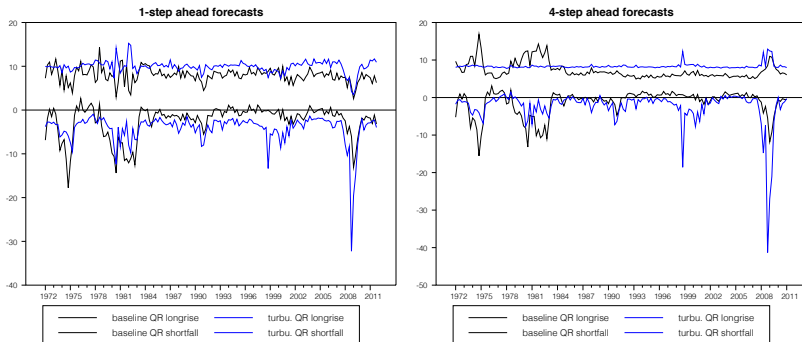
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BVARs with time-varying volatility offer a viable alternative

- BVARs broadly useful for forecasting (point forecasts, scenario analysis, etc.)
- Single model can cover all variables, horizons, and quantiles of interest
- Need time-varying volatility to get shifts in conditional variances

# Robustness results using turbulence: Predictive distributions

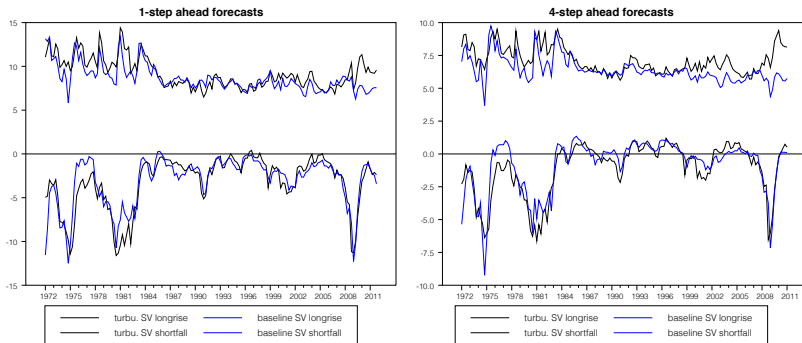
Expected longrise and shortfall: GDP growth  
baseline QR vs. turbu. QR



- QR: Replacing NFCI with turbulence greatly increases ES variability (even more so OOS)

# Robustness results using turbulence: Predictive distributions

Expected longrise and shortfall: GDP growth  
turbu. BVAR-SV vs. baseline BVAR-SV



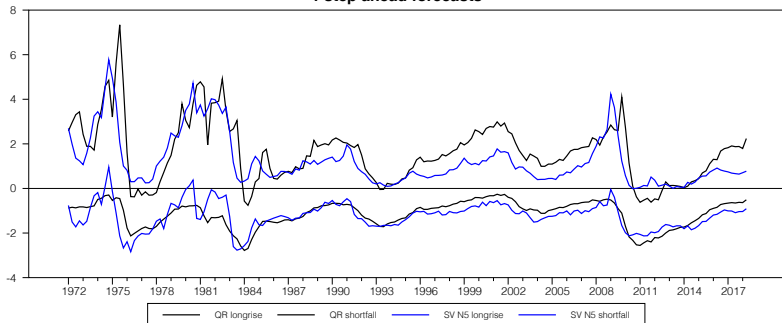
- BVAR-SV: Estimates similar with turbulence as compared to NFCI



# Robustness results using unemployment: Predictive distributions

Expected longrise and shortfall: 4-quarter UR change  
QR vs. BVAR-SV, N=5

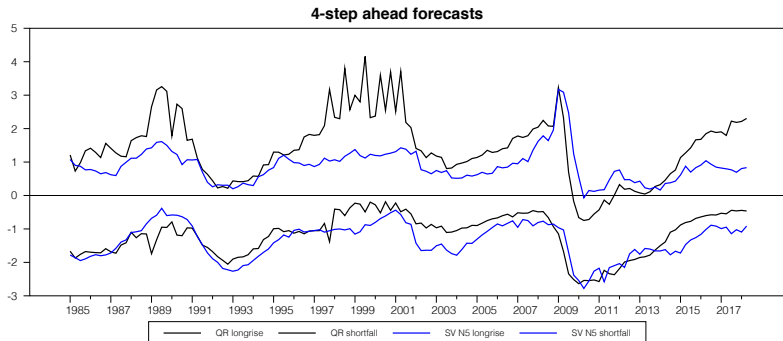
4-step ahead forecasts



- In-sample estimates show considerable time variation in upside risk
- LR more variable than ES
- Contours of QR and BVAR-SV estimates are similar

# Robustness results using unemployment: Predictive distributions

Expected longrise and shortfall: 4-quarter UR change  
QR vs. BVAR-SV, N=5



- Evidence of asymmetries in LR vs. ES is somewhat weaker out-of-sample
- Considerable choppiness of QR estimate in 1990s

# Robustness results using unemployment: Accuracy of in-sample forecasts

	<b>BVAR-SV/QR</b>	
	1985-2018	1985-2007
5% QS	1.010	0.825
5% VaR-ES	0.060	0.092
	<b>BVAR-GFSV/QR</b>	
	1985-2018	1985-2007
5% QS	1.045	0.825
5% VaR-ES	0.050	0.097

- In-sample tail risk forecasts: SV and GFSV estimates about as accurate as QR

# Robustness results using unemployment: Accuracy of out-of-sample forecasts

	<b>BVAR-SV/QR</b>	
	1985-2018	1985-2007
5% QS	1.092	1.125
5% VaR-ES	-0.014	-0.069
	<b>BVAR-GFSV/QR</b>	
	1985-2018	1985-2007
5% QS	1.096	1.121
5% VaR-ES	-0.039	-0.074

- Out-of-sample tail risk forecasts: SV and GFSV estimates about as accurate as QR

# Conclusions

In general, a BVAR-SV model performs as well as quantile regression in measuring and forecasting tail risks to economic activity

- Key features for BVAR: time-varying volatility and inclusion of financial conditions
- Captures simultaneous shifts in conditional means and variances

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In general, a BVAR-SV model performs as well as quantile regression in measuring and forecasting tail risks to economic activity

- Key features for BVAR: time-varying volatility and inclusion of financial conditions
- Captures simultaneous shifts in conditional means and variances

## Key findings:

- Statistical evidence of skewness in output growth is generally weak
- QR-based approaches can come with some challenges in macro data samples: quantile crossing and coefficient variability
- BVAR-SV models are able to capture time variation in output tail risks — with downside risks more variable than upside risks — like that emphasized in ABG
- BVAR-SV scores as well as QR for downside tail risks