Can Deficits Finance Themselves?

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How Are Deficits Financed? [r > g]

$$\frac{B_0}{P_0} = \mathsf{PV} \text{ of Surpluses} = f(\mathsf{tax rate} \times \mathsf{tax base}, \cdots)$$

Basic answer: Fiscal adjustment: raise tax rate in the future

This paper: Self-financing with finite lives/liquidity constraints [HANK, OLG, ...]

- Deficit \Rightarrow Keynesian boom \Rightarrow tax base \uparrow and debt erosion ($P_0 \uparrow$)
 - improve budget without tax rate/spending adjustment
- Q: How important is such self-financing? can there ever be full self-financing?

How Big Can "Self-financing" Be?

Environment: finite lives/liquidity constraints + nominal rigidities

Policy: full fiscal adjustment promised at future date H + monetary policy "neutral" (fix $\mathbb{E}[r]$))

- Main result: complete self-financing by delaying fiscal adjustment
 - Monotonicity: as H increases, the actual required future tax hike gets smaller and smaller
 - · Limit: the future tax hike vanishes, i.e., we converge to full self-financing
 - Split depends on price rigidities. [All via tax base \uparrow if rigid, all via prices \uparrow if approx. flexible.]

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 - · Limit: the future tax hike vanishes, i.e., we converge to full self-financing
 - Split depends on price rigidities. [All via tax base \uparrow if rigid, all via prices \uparrow if approx. flexible.]
- Intuition: finite-lives/liq. constraints: "discount" far-future tax & front-loaded Keynesian cross
- Difference from FTPL: not by the force of eq'm selection [no threat to violate government budget]
- **Practical relevance**: holds in many environments & quantitatively powerful [general AD (incl. HANK), active monetary policy, investment, distortionary taxation, ...]

Outline

Environment: OLG-NK

- 2 Equilibrium Characterization
- Self-financing of Fiscal Deficits
- Extensions & Generality
- 5 Conclusion

Households and Firms

Perpetual youth consumers with survival rate ω [ω = 1: RANK; ω < 1: proxy for HANK, later]

$$\mathbb{E}_t\left[\sum_{k=0}^{\infty} \left(\beta \omega\right)^k \left[u(C_{i,t+k})-v(L_{i,t+k})\right]\right],$$

• Invests in actuarially fair annuities [transfer to newborns: all cohorts have same C in steady state].

$$A_{i,t+1} = \underbrace{\frac{I_t}{\omega}}_{\text{annuity}} \left(A_{i,t} + P_t \cdot \left(\underbrace{\frac{W_t L_{i,t} + Q_{i,t}}{Y_{i,t}}}_{Y_{i,t}} - C_{i,t} - T_{i,t} + \text{Transfer to Newborns} \right) \right)$$

• Abstract from income heterogeneity: $Y_{i,t} = Y_t$ and $T_{i,t} = \mathscr{T}_t(Y_{i,t}) = T_t$ · Details

• Key features with $\omega < 1$ [(i) elevated MPC + (ii) discounting future income & taxes, breaking Ricardian Equiv.]

Firms as in textbook NK model: standard NKPC [in log: $\pi_t = \kappa y_t + \beta \mathbb{E}_t[\pi_{t+1}]$]

Policy, Market Clearing, and Log-Linearization

• Government budget [no G_t , T_t is the primary surplus]

$$\frac{1}{l_t}B_{t+1} = B_t - P_t T_t \qquad (\text{plus no Ponzi})$$

and define $D_t = B_t/P_t$ as real value of public debt outstanding.

• Market clearing
$$Y_t = \int C_{i,t} di$$
 and $\int A_{i,t} di = B_t.$

Initial condition

$$A_{i,0}=B_0$$

• Log-linearization: a lower case capture log-deviations from steady state [with the exception of fiscal variables, e.g., $d_t = \frac{d_t - D^{SS}}{V^{SS}}$, to accommodate $D^{SS} = 0$

Monetary Policy

• Baseline: no monetary accommodation [expected real rate in variant to debt & deficit]

$$r_t \equiv i_t - E_t[\pi_{t+1}] = 0$$

• Extension: different degrees of monetary accommodation

$$r_t = \phi y_t$$

- $\phi < 0$: an "accommodative" monetary authority
- $\phi > 0$: leans against the wind

Fiscal Policy

• Baseline: Markovian Fiscal Policy [extension of Leeper (1991)]

$$T_{i,t} = T_t = \overline{T} + \tau_d \left(D_t + \mathscr{E}_t \right) + \tau_y Y_{i,t} - \mathscr{E}_t,$$

or after (log-)linearization



(1)

(2)

- $au_d \in [0,1]$: a lower au_d captures delay in fiscal adjustment
- $\tau_{y} > 0$: self financing through endogenous adjustment in tax base
- Variant: a Non-Markovian FP with delayed full fiscal adjustment

$$t_t = \begin{cases} \tau_y y_t - \varepsilon_t & t < H & \text{initially no fiscal adjustment} \\ d_t & t \ge H & \text{eventually full fiscal adjustment} \end{cases}$$

• High H, similar to low τ_d , captures delay in fiscal adjustment

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Aggregate Demand

• Optimal consumption + aggregation $[\gamma \equiv \sigma\beta\omega - (1 - \beta\omega)\beta\frac{D^{ss}}{Y^{ss}}]$

$$c_{t} = \underbrace{(1 - \beta \omega)}_{\mathsf{MPC}} \times \left(\underbrace{a_{t}}_{\mathsf{wealth}} + \underbrace{\mathbb{E}_{t}\left[\sum_{k=0}^{\infty} (\beta \omega)^{k} (y_{t+k} - t_{t+k})\right]}_{\mathsf{post-tax income}} - \underbrace{\gamma \mathbb{E}_{t}\left[\sum_{k=0}^{\infty} (\beta \omega)^{k} r_{t+k}\right]}_{\mathsf{real rates}}\right)$$

• Using monetary, fiscal policy and market clearing

$$y_t = \mathscr{F}_1 \cdot (d_t + \varepsilon_t) + \mathscr{F}_2 \cdot E_t \left[\sum_{k=0}^{+\infty} (\beta \omega)^k y_{t+k} \right],$$

(3)

with $\mathscr{F}_1 = \frac{(1-\beta\omega)(1-\omega)(1-\tau_d)}{1-\omega(1-\tau_d)}$ and $\mathscr{F}_2 = (1-\beta\omega)\left(1-\tau_y\frac{1-\omega}{1-\omega(1-\tau_d)}\right).$

- \mathscr{F}_1 captures PE effect of debt/deficits on AD
 - * $\mathscr{F}_1 > 0$ iff $\omega < 1$ (failure of Ricardian Equiv)
 - * deficits are transfer from future generations to current generations
- \mathscr{F}_2 captures GE effect through intertemporal Keynesian cross
 - * jointly governed by FP (τ_d and τ_y), and MPC (ω)

The economy in 3 equations

1 AD:

$$y_t = \mathscr{F}_1 \cdot (d_t + \varepsilon_t) + \mathscr{F}_2 \cdot \mathbb{E}_t \left[\sum_{k=0}^{+\infty} (\beta \omega)^k y_{t+k} \right],$$

AS:

$$\pi_t = \kappa y_t + \beta \mathbb{E}_t \left[\pi_{t+1} \right]$$

② Evolution of real value of public debt:

$$d_{t+1} = \beta^{-1} (d_t - t_t) - \underbrace{\frac{D^{ss}}{\gamma_{ss}} (\pi_{t+1} - \mathbb{E}_t [\pi_{t+1}])}_{\text{self financing: debt erosion}}$$
with
$$t_t = \underbrace{\tau_d \cdot (d_t + \varepsilon_t)}_{\text{fiscal adjustment}} + \underbrace{\tau_y y_t}_{\text{self financing: tax base}} - \varepsilon_t$$

Equilibrium Existence and Uniqueness

Theorem

Let $\omega < 1$ and $\tau_{\gamma} > 0$. There exists **unique bounded eq'm** taking the form:

$$y_t = \chi(d_t + \varepsilon_t), \quad E_t[d_{t+1}] = \rho_d(d_t + \varepsilon_t).$$

Moreover, $\chi > 0$ (deficits trigger boom) and $0 < \rho_d < 1$ (debt converges to steady state).

- Finding the equilibrium: fixed-point relation $ho_d\longleftrightarrow\chi$
 - $\chi
 ightarrow
 ho_d$ follows from the evolution of real value of public debt:

$$\rho_d = \frac{1}{\beta} \left(1 - \tau_d - \tau_y \chi \right)$$

• $ho_d
ightarrow \chi$ follows from the aggregate demand/IKC

$$\chi = \mathscr{F}_1/\left(1 - \mathscr{F}_2/\left(1 - \beta \omega \rho_d\right)\right)$$



Environment: OLG-NK

2 Equilibrium Characterization

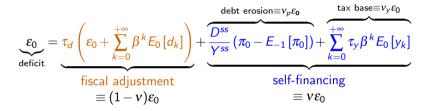
Self-financing of Fiscal Deficits

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Channels of Self Financing

- Start with $d_0 = 0$ (steady state) and consider $\varepsilon_0 > 0$ (MIT positive deficit shock)
- Gov's intertemporal budget constraint \Rightarrow



where $v \equiv$ fraction of deficit that is self-financed, contrast with fiscal adjustment.

- RANK benchmark ($\omega = 1$)
 - **③** Standard eq'm ($\phi \rightarrow 0^+$): zero self financing, v = 0
 - FTPL: full self financing v = 1 through the force of eq'm selection [non-Ricardian FP, threat to violate government budget]
- Now ($\omega < 1$): Full self financing with delayed fiscal adjustment $[\tau_d \rightarrow 0 \text{ or } H \rightarrow +\infty]$

The Self Financing Result

Theorem

Suppose that $\omega < 1$ and $\tau_y > 0$.

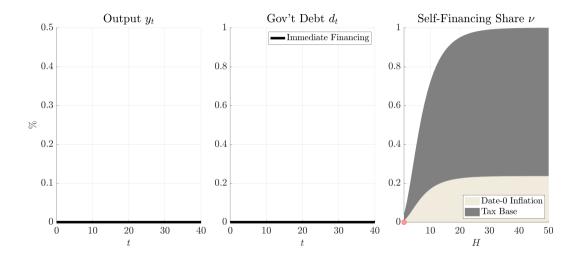
(Monotonicity) Self-financing share v increases in the delay of fiscal adjustment (i.e., it is increasing in H and decreasing in τ_d).

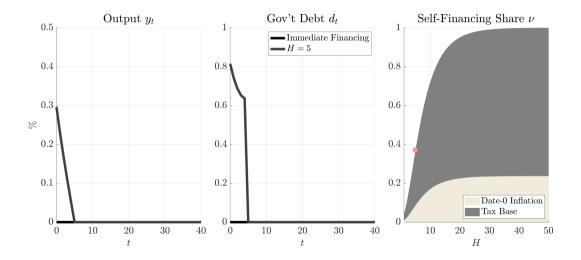
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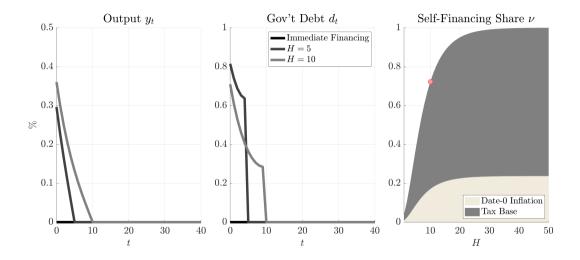
Theorem

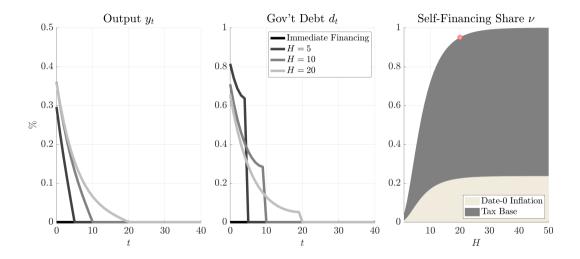
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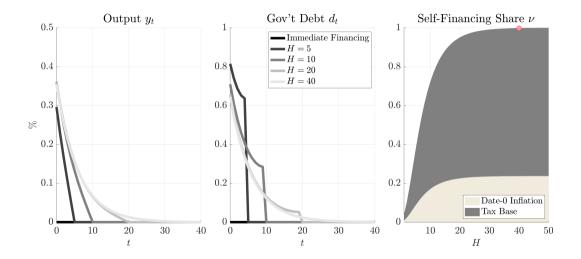
- **(Monotonicity)** Self-financing share v increases in the delay of fiscal adjustment (i.e., it is increasing in H and decreasing in τ_d).
- [Limit] As fiscal financing is delayed further (i.e., as H→∞ or τ_d→0), there is complete self financing: ν converges to 1.
 - In this limit, self-financing is strong enough to return d to SS without any fiscal adjustment. $[\tau_d \rightarrow 0: \lim_{k \rightarrow \infty} \mathbb{E}_t[d_{t+k}] \rightarrow 0; H \rightarrow \infty: \lim_{H \rightarrow \infty} \mathbb{E}_0[d_H] \rightarrow 0]$



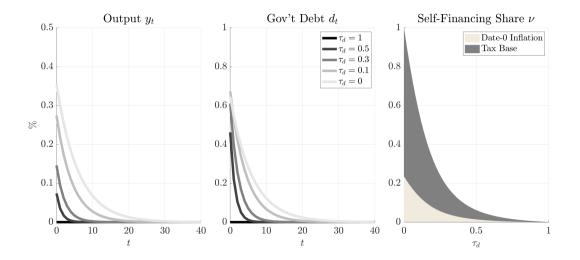








A Graphical Illustration $[t_t = \tau_d (d_t + \varepsilon_t) + \tau_y y_t - \varepsilon_t]$



Economic Intuition [Fully Rigid Price, $\kappa = 0$]

• To illustrate consider the total adj. of tax base from static Keynesian cross

$$c = \mathsf{MPC} \cdot y_{\mathsf{disp}} \text{ and } y_{\mathsf{disp}} = (1 - \tau_y)y + \varepsilon \Longrightarrow y = \frac{\mathsf{MPC}}{1 - (1 - \tau_y)\mathsf{MPC}} \times \varepsilon$$

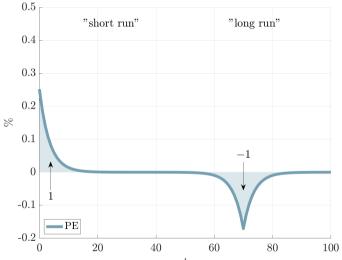
- \$1 increase in transfer leads to \$MPC increase in AD
- \$1 increase in AD leads to $(1 \tau_y)$ GE increase in post-tax income
- $(1 \tau_y)$ increase in post-tax income lead to $MPC \times (1 \tau_y)$ increase in AD
- Self-financing through tax base adjustment: $v \equiv \frac{\tau_y y}{\epsilon} = \frac{\tau_y MPC}{1 (1 \tau_y)MPC}$ is increasing in the MPC
 - future tax hike needed: $R(1-v)\varepsilon$
- Full self-financing would require MPC = 1, giving $y = \frac{1}{\tau_y} \times \mathcal{E}$. [Hint: Dynamic: cumulative MPC = 1]

Our th'm: features of static model have analogues in dynamic economy

1. Static: expected "future" tax hike does not affect "current" spending behavior \implies Dynamic: discount ($\omega < 1$) \implies far future *H*-tax's impact on short-run consumption vanishes

[IKC matrix: income change at $t + \ell$ has a vanishing effect on t consumption: $\lim_{\ell \to \infty} \beta^{-\ell} \mathscr{M}_{t,t+\ell} = 0$]

Economic Intuition [$\kappa = 0$, PE effect of tax-and-transfer vector $\mathcal{M} \cdot t^{PE}$, with $t^{PE} = (-1, \dots, \beta^{-H})$]



t

Economic Intuition [Fully Rigid Price, $\kappa = 0$]

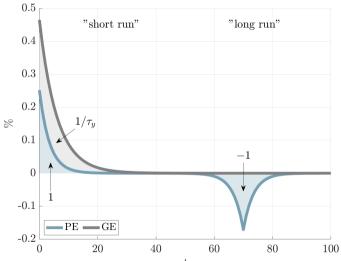
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- 2. Static: "current" transfer & additional GE income are fully spent currently (MPC ightarrow 1)
 - \implies Dynamic: front-loaded MPCs (ω < 1) \implies cumulative short-run MPCs approach 1 far before H

[IKC matrix: income change at $t + \ell$ has a vanishing effect on t consumption: $\lim_{\ell \to \infty} \beta^{-\ell} \mathscr{M}_{t,t+\ell} = 0$]

- \implies Transfer receipt (and higher-order GE income) is spent quickly
- \implies Thus debt stabilizes on its own before *H*, and tax hike is not needed.

Economic Intuition [$\kappa = 0$, PE and GE effect of tax-and-transfer vector]



t

Economic Intuition: The Role of Nominal Rigidities, $\kappa > 0$

A simple rescaling of the perfect rigid price case $\kappa=0$

• From NKPC, self financing through tax base is **proportional** to through debt erosion:

$$\pi_0 - E_{-1}[\pi_0] = \kappa \cdot \mathsf{NPV}(y) = \kappa \cdot \sum_{k=0}^{+\infty} \beta^k E_0[y_k]$$

• Split between sources of self financing:

tax base:
$$v_y = \frac{\tau_y}{\tau_y + \kappa \frac{D^{ss}}{Y^{ss}}} v$$
 & debt erosion: $v_p = \frac{\kappa \frac{D^{ss}}{Y^{ss}}}{\tau_y + \kappa \frac{D^{ss}}{Y^{ss}}} v$

DEC

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-

• When price is appr. flexible $(\kappa \to +\infty)$, full self financing through debt erosion $(\nu_p \to 1)$

- Infinitesimal boom leads to large enough adjustment in P_0 to finance ε_0
- Akin to FTPL, but from deficit-driven Keynesian boom [not by the force of eq'm selection, no threat to violate government budget]

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Extensions & Generality

- Fiscal policy
 - limit result unaffected if far-ahead adjustment is distortionary
 - result applies with little change to gov't purchases instead of transfers
- More general aggregate demand [coming up]
- Monetary policy [coming up]
- Allow for investment, limit result unaffected [same IKC among consumers]

A Generalized Aggregate Demand Relation

- Our results are not tied to the particular OLG microfoundations
- Consider the following generalized AD relation:

$$c_t = M_d d_t + M_y \left(y_t - t_t + \delta \mathbb{E}_t \left[\sum_{k=0}^{\infty} (\beta \omega)^k (y_{t+k} - t_{t+k}) \right]
ight)$$

[Rich enough to nest PIH, OLG, spender-saver, spender-OLG, behavioral discounting, ...]

Complete self-financing with two empirically plausible features of consumer demand
 Discounting: far future tax hike's impact on current consumption vanishes

$$\omega < 1.$$
 (4)

(5)

Front-loaded MPCs: transfer receipt (and higher-order GE income) is spent quickly

$$M_d + rac{1-eta}{ au_y} \left(1- au_y
ight) M_y \left(1+\delta\sum_{k=1}^\infty \left(eta\,\omega
ight)^k
ight) > rac{1-eta}{ au_y}.$$

[Deficit-driven Keynesian boom is front-loaded enough to deliver $\rho_d < 1$.]

A Generalized Aggregate Demand Relation

Theorem

Under (4) and (5).

- As fiscal financing is delayed further (i.e., as H→∞ or τ_d→0), there is complete self financing: ν converges to 1.
- In this limit, self-financing is strong enough to return d to SS without any fiscal adjustment. $[\tau_d \rightarrow 0: \lim_{k \rightarrow \infty} \mathbb{E}_t[d_{t+k}] \rightarrow 0; H \rightarrow \infty: \lim_{H \rightarrow \infty} \mathbb{E}_0[d_H] \rightarrow 0]$
- Models satisfy both assumptions: OLG OLG-spender, behavioral discounting
- Models violate either assumptions: PIH, spender-saver

[Discounting fails. Empirically unrealistic, infinite elasticity of household asset demand to interest rates]

Different Degrees of Monetary Accommodation • Leeper Regions

• Extension: OLG + a Real Taylor Rule

 $r_t = \phi y_t$

[baseline $\phi = 0$; $\phi < 0$ accelerates the deficit-driven boom; $\phi > 0$ delays it]

Proposition

There exists $\bar{\phi} > 0$, such that, iff $\phi \leq \bar{\phi}$, there is **full self financing** with **infinitely delayed fiscal adjustment**.

- Complete self-financing if MP does not lean against the boom "too aggressively."
- What happens if $\phi > \overline{\phi}$?
 - No bounded *complete* self financing eq'm exists (with $au_d
 ightarrow 0$)
 - If fiscal adjustment is fast enough (with $\tau_d > \overline{\tau}_d(\overline{\phi})$), there is bounded *partial* self financing eq'm.

Key targets: (i) consumer spending behavior [iMPCs] & (ii) fiscal adjustment speed

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[Why? disentangles level & slope of dynamic MPC profile, consistent with evidence.]

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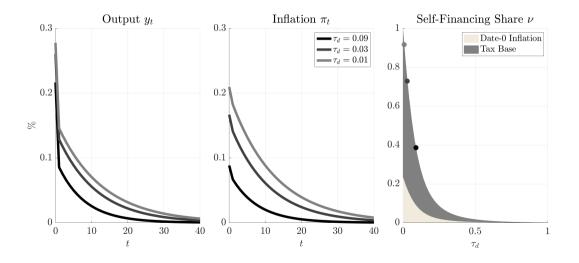
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[Why? disentangles level & slope of dynamic MPC profile, consistent with evidence.]

Calibration strategy

- Match evidence on iMPCs to lump-sum income receipt in Fagereng-Holm-Natvik [Later: other calibration targets, behavioral models, and a full-blown HANK model...]
- Consider range of τ_d consistent with literature on fiscal adjustment rule estimation [Galí-López-Salido-Vallés, Bianchi-Melosi, Auclert-Rognlie, ...]

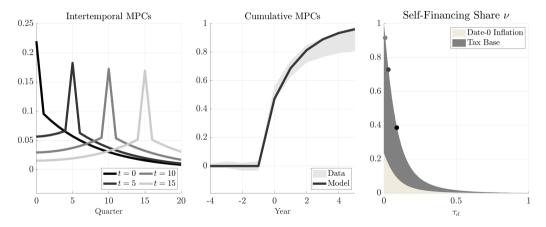
Application: Stimulus Checks



Alternative Calibration Strategies • hank • behavioral

Baseline: match impact and short-run MPCs, then extrapolate

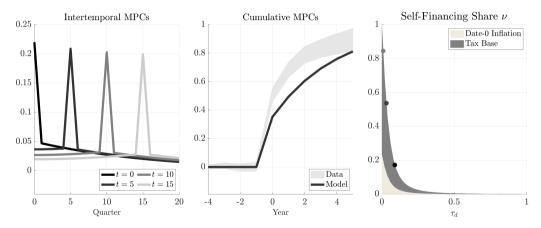
[This gives $\omega = 0.88$]



Alternative Calibration Strategies (hank (behavioral

Variant I: match lower bound of six-year cumulative spending share

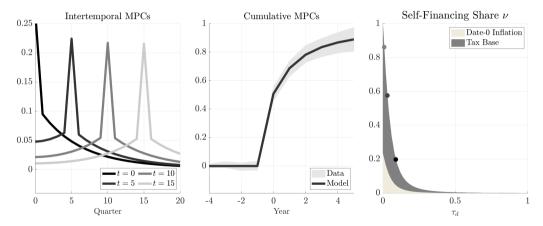
[This gives $\omega = 0.96$, and thus counterfactually elastic hh asset demand to $r \ (\approx 6x \text{ emp. upper bound})$.]



Alternative Calibration Strategies (hank (behavioral

Variant II: two-type OLG + spender model to match cumulative MPC time profile

[This gives $\omega_2 = 0.97$, and thus again counterfactually elastic hh asset demand to $r \ (\approx 7x \text{ emp. upper bound})$.]



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• Key: delayed fiscal adjustment \Rightarrow strong self-financing from tax base adjust. & debt erosion

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Implications:

- Theory: grounded in a failure of Ricardian equivalence + nominal rigidities [robust to info perturbations, consistent with Taylor principle, no threat to violate gov. budget]
- **②** Practice: self-sustaining stimulus may be less implausible than commonly believed

Conclusion

• Key: delayed fiscal adjustment \Rightarrow strong self-financing from tax base adjust. & debt erosion

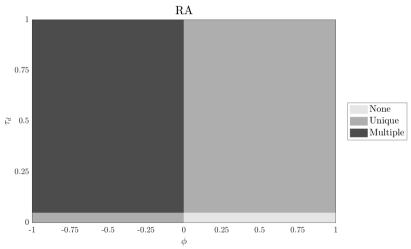
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- Theory: grounded in a failure of Ricardian equivalence + nominal rigidities [robust to info perturbations, consistent with Taylor principle, no threat to violate gov. budget]
- **②** Practice: self-sustaining stimulus may be less implausible than commonly believed
- Future work: (optimal) policy implications for fiscal-monetary interaction

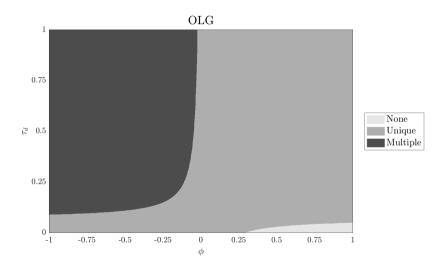
• Unions equalize post-tax wage and average consumption-labor MRS. This gives

$$(1- au_y)W_t=rac{\chi L_t^{rac{1}{arphi}}}{\int_0^1 C_{i,t}^{-1/\sigma} di}$$
 and $L_{i,t}=L_t.$

Leeper Regions •••••

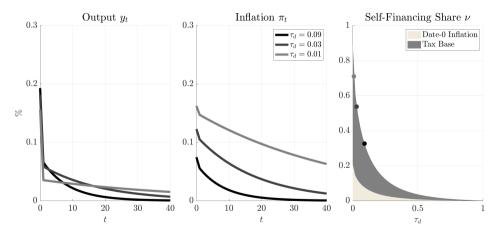


Leeper Regions •••••



Behavioral Households (Cognitive Discounting)

Main result: large initial boom [bigger PE] but slower convergence [dampen GE]



A Simple Hank Model •••••

• Environment: standard one-asset HANK model

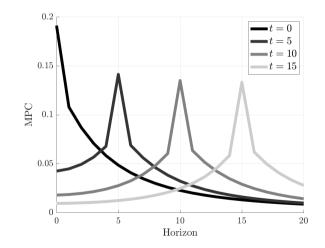
[As in McKay-Nakamurs-Steinsson (2016), Auclert-Rognlie-Straub (2018), Wolf (2022): self-insure against idiosyncratic earnings risk through savings in a single risk-free asset.]

• Calibration

- Income risk process: taken straight from Kaplan-Moll-Violante (2018)
- 3 Tax-and-transfer system: $\tau_y = 0.3$, $\frac{\text{transfer}}{v} = 0.07$ [also as in Kaplan-Moll-Violante (2018)]
- **O** Total wealth: calibrate to U.S. economy liquid wealth/income ratio
- GE income incidence: uniform [note that this is conservative for our purposes]

implies: average MPC somewhat below 0.3

A Simple Hank Model • main



A Simple Hank Model • main

